



Figure 3.8: Graph of the function $f(x) = \sin x - x \cos x$ on the interval $[-1, 8]$, showing the three roots of the equation $\sin x - x \cos x = 0$ in that interval.

method. However, to illustrate what can go wrong, consider using $x_0 = 6$ in the present example. The algorithm produces a sequence of approximations that converges to the root $x = 0$, rather than the root $x = r \approx 4.4934$. This may have surprised you! The plot in Figure 3.10 graphically illustrates this.

Exercise Set 3

1. The following are variations of the code used in Examples 3.1–3.2 to compute Riemann sums. Analyze what each does and give the mathematical formula for what it is actually computing.

N := 10

(a) $dX := (b-a)/N$; $X := a$; $Y := f(a)$; $s := 0$;

for i from 1 to N do

$X := X + dX$; $Y := f(X)$;

$s := s + Y * dX$;

end do;

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(b) $X := \text{array}(0..N)$; $Y := \text{array}(0..N)$;

$dX := (b-a)/N$; $X[0] := a$; $Y[0] := f(X[0])$; $s := 0$;

for i from 1 to N do

$X[i] := X[i-1] + dX$; $Y[i] := f(X[i])$;

$s := s + Y[i-1] * dX$;

end do;

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2. (Riemann Sums) As in Example 3.2, write some code to compute the Riemann sum approximations and draw the outline (boundary) of the approximating areas for the following situations.