



Figure 3.9: For initial approximation  $x_0 = 5.5$ , Newton's method converges to the root  $r \approx 4.4934$ .

- (i) **(Right-Hand Rule)** For the  $i$ th rectangle on the interval  $[x_{i-1}, x_i]$ , use the value  $f(x_i)$  at the right-hand endpoint for the height of the rectangle.
- (ii) **(Midpoint Rule)** For the  $i$ th rectangle on the interval  $[x_{i-1}, x_i]$ , use the value  $f(m_i)$  at the midpoint  $m_i = (x_{i-1} + x_i)/2$ , for the height of the rectangle.

Apply your code to the functions that you are assigned from the following.

- (a)  $f(x) = x^2 - x^4 + 1$  on the interval  $[0, 1]$  (this is from Example 3.2).
- (b)  $f(x) = 1 + x^{\sin x}$  on the interval  $[1, 5]$ .
- (c)  $f(x) = 1 + e^{-x} \sin 10x$  on the interval  $[0, 2]$ .
- (d)  $f(x) = 1 + \sin 10x \sin x$  on the interval  $[0, 2]$ .

In each case, do the Riemann sum approximations and graphics for  $N = 10, 30, 50, 100$ . Annotate your graphics with the value of  $N$  and the corresponding value of the approximating Riemann sums. Use Maple to compute a good floating-point approximation to the true value of the definite integral. If you are assigned (c) or (d), compute the exact value by hand. Show your work!

3. **(Alternating Series)** At the end of the discussion in Example 3.3, we made the claim that the alternating series being studied numerically had an exact value for its sum:

$$\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n(n+1)} = 2 \ln 2 - 1.$$