

$$\left(\beta \int_0^1 \left(\frac{\partial \bar{w}}{\partial \bar{x}} \right)^2 d\bar{x} \right) \frac{\partial^2 \bar{w}}{\partial \bar{x}^2} - (1 + \gamma) \frac{\partial^4 \bar{w}}{\partial \bar{x}^4} + \alpha \frac{\partial^2}{\partial \bar{x}^2} \left[\left(\phi \left(\bar{x}, \frac{1}{2} \right) - \phi \left(\bar{x}, -\frac{1}{2} \right) \right) \right] + \bar{q} = 0 \quad (39)$$

$$\frac{\partial^2 \phi}{\partial \bar{x}^2} + \left(\frac{L}{h} \right)^2 \frac{\partial^2 \phi}{\partial \bar{z}^2} = 0 \quad (40)$$

$$\bar{w} \Big|_{\bar{x}=0,1} = 0 \quad (41)$$

$$\left[-(1 + \gamma) \frac{\partial^2 \bar{w}}{\partial \bar{x}^2} + \alpha \left(\phi \Big|_{-1/2}^{1/2} \right) \right]_{\bar{x}=0,1} = 0 \quad (42)$$

$$\left[\left(\frac{L}{h} \right) \frac{\partial \phi}{\partial \bar{z}} + \eta \frac{\partial^2 \bar{w}}{\partial \bar{x}^2} \right]_{\bar{z}=-1/2,1/2} = 0 \quad (43)$$

$$\phi \Big|_{\bar{x}=0,1} = 0 \quad (44)$$

In the above equations, the constants are expressed as:

$$\beta = \frac{Mh^2L}{(\lambda + 2\mu)I}, \quad \alpha = \frac{2bfL^2}{(\lambda + 2\mu)Ih}, \quad \gamma = \frac{4\mu A l^2}{(\lambda + 2\mu)I}, \quad \bar{q} = \frac{q_0 L^4}{(\lambda + 2\mu)I}, \quad \eta = \frac{fh}{\varepsilon_0 L} \quad (45)$$

$$M = \frac{(\lambda + 2\mu)A}{2L}, \quad K = (\lambda + 2\mu)I + 4\mu A l^2$$

Where

$$> E := 107.8077e9;$$

$$E := 1.07807710^{11}$$

$$> nu := 0.2565;$$

$$\nu := 0.2565$$

$$> epsilon := 8.85e-12;$$

$$\varepsilon := 8.85 \cdot 10^{-12}$$

$$> q0 := 0.02;$$

$$q := 0.02$$

>

$$> f := 5e-12;$$

$$f := 5 \cdot 10^{-12}$$

$$> landa := \frac{E \cdot nu}{((1 + nu) \cdot (1 - 2 \cdot nu))};$$

$$landa := 4.51903490810^{10}$$

$$> miu := \frac{E}{(2 \cdot (1 + nu))};$$

$$miu := 4.29000000010^{10}$$

$$> b := 10e-9;$$

$$b := 1.0 \cdot 10^{-8}$$

$$> h := 15e-9;$$

$$h := 1.5 \cdot 10^{-8}$$

$$> l := 0.2 \cdot h;$$

$$l := 3.0 \cdot 10^{-9}$$

>

$$> I := \frac{b \cdot h^3}{12};$$

$$I := 2.81250000010^{-33}$$

$$> A := b \cdot h;$$

$$A := 1.50 \cdot 10^{-16}$$

$$> L := 300e-9;$$