

$$S(n) = \sum_{i=1}^n \left(\prod_{j=i}^n \frac{1}{j^i} \right)$$